Query Optimization Exercise Session 3

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November 21

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```
select *
from lineitem l, orders o, customers c
where l.l_orderkey=o.o_orderkey
and o.o_custkey=c.c_custkey
and c.c_name='Customer#000014993'.
```

We know |R1|, |R2|, domains of R1.x, R2.y,

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▶ if *x* is the key:

• if x is the key:  $\frac{1}{|R1|}$ 

- if x is the key:  $\frac{1}{|R1|}$
- if x is not the key:

- if x is the key:  $\frac{1}{|R1|}$
- if x is not the key:  $\frac{1}{|R1.x|}$

We know |R1|, |R2|, |R1.x|, |R2.y|, and whether x and y are keys or not. First, the size of  $R1 \times R2$  is

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First, the size of  $R1 \times R2$  is |R1||R2|

The selectivity of  $\bowtie_{R1.x=R2.y}$  is...

if both x and y are the keys:

First, the size of  $R1 \times R2$  is |R1||R2|

The selectivity of  $\bowtie_{R1.x=R2.y}$  is...

• if both x and y are the keys:  $\frac{1}{\max(|R1|, |R2|)}$ 

- if both x and y are the keys:  $\frac{1}{\max(|R1|, |R2|)}$
- ▶ if only *x* is the key:

- if both x and y are the keys:  $\frac{1}{\max(|R1|,|R2|)}$
- if only x is the key:  $\frac{1}{|R1|}$

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- if both x and y are not the keys:  $\frac{1}{max(|R1.x|,|R2.y|)}$

The selectivity of  $\sigma_{R1.x>c}$  is



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The selectivity of 
$$\sigma_{R1.x>c}$$
 is  $\frac{max(R1.x)-c}{max(R1.x)-min(R1.x)}$ 

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The selectivity of 
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The selectivity of  $\sigma_{c1 < R1.x < c2}$  is

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 is  $\frac{max(R1.x)-c}{max(R1.x)-min(R1.x)}$ 

The selectivity of  $\sigma_{c1 < R1.x < c2}$  is  $\frac{c2-c1}{max-min}$ 

- ▶ |R| = 1,000 pages, |S| = 100,000 pages
- 1 page 50 tuples, 1 block 100 pages
- ▶ avg. access = 10 ms, transfer speed = 10,000 pages/sec

Time for blocked nested loops join = ?

- ▶ |R| = 1,000 pages, |S| = 100,000 pages
- 1 page 50 tuples, 1 block 100 pages
- ▶ avg. access = 10 ms, transfer speed = 10,000 pages/sec

- Time for blocked nested loops join = ?
- ▶ choose left argument: *R* vs. *S*,  $\frac{1,000}{100}$  vs.  $\frac{100,000}{100} \Rightarrow R$

• Time to read one block:  $T_b = avg.seek + (100 \frac{1}{\text{transfer speed}}) = 0.02s$ 

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Time to read one block:  $T_b = avg.seek + (100\frac{1}{transfer speed}) = 0.02s$ 

▶ Read 1 block from *R*, join it with *S*:

 $T_b$  + time to read S  $\approx 10s$ 

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 Time to read one block: T<sub>b</sub> = avg.seek + (100<sup>1</sup>/<sub>transfer speed</sub>) = 0.02s

 Read 1 block from *R*, join it with *S*:

 $T_b$  + time to read S  $\approx 10s$ 

Repeat it for every block in R:

$$T_{BNLJ} = rac{\# pages in R}{block size} (10s) pprox 100s$$

## Greedy operator ordering

- take the query graph
- ▶ find relations R<sub>1</sub>, R<sub>2</sub> such that |R<sub>1</sub> ⋈ R<sub>2</sub>| is minimal and merge them into one node

repeat until the query graph has more than one node

Generates bushy trees!

Example



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Example - step 1



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#### Example - after step 1



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Example - step 2



#### Example- after step 2



Example - step 3



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#### Example - after step 3



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Example - step 4



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Example - after step 4



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#### Example - step 5



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Example - after step 5

# $(R_{1} \bowtie R_{2}) \bowtie (R_{3} \bowtie R_{4})(1200)$ 0.2268 $(R_{7} \bowtie R_{8}) \bowtie ((R_{5} \bowtie R_{6}) \bowtie R_{9})(1080)$

# Example - result



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# IKKBZ (informally)

Query graph Q is acyclic. Pick a root node, turn it into a tree. Run the following procedure for every root node, select the cheapest plan

Input: rooted tree Q

- 1. if the tree is a single chain, stop
- 2. find the subtree (rooted at r) all of whose children are chains
- 3. normalize, if  $c_1 \rightarrow c_2$ , but  $rank(c_1) > rank(c_2)$  in the subtree rooted at r

- 4. merge chains in the subtree rooted at r, rank is ascending
- 5. repeat 1

# IKKBZ (informally)

For every relation  $R_i$  we keep

- cardinality n<sub>i</sub>
- selectivity s<sub>i</sub> the selectivity of the incoming edge from the parent of R<sub>i</sub>

• cost  $C(R_i) = n_i s_i$  (or 0, if  $R_i$  is the root)

• rank 
$$r_i = \frac{n_i s_i - 1}{n_i s_i}$$

Moreover,

- $C(S_1S_2) = C(S_1) + T(S_1)C(S_2)$
- $T(S) = \prod_{R_i \in S} (s_i n_i)$
- rank of a sequence  $r(S) = \frac{T(S)-1}{C(S)}$

#### Understanding IKKBZ

- what is the rank?
- when is  $(R_1 \bowtie R_2) \bowtie R_3$  cheaper than  $(R_1 \bowtie R_3) \bowtie R_2$ ?

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### Understanding IKKBZ

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• if  $r(R_2) < r(R_3)!$ 



Relation	n	S	С	Т	rank
2	20	$\frac{1}{5}$	4	4	$\frac{3}{4}$
3	30	$\frac{1}{3}$	10	10	$\frac{9}{10}$
4	50	$\frac{1}{10}$	5	5	$\frac{4}{5}$
5	2	1	2	2	$\frac{1}{2}$

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3	30	$\frac{1}{3}$	10	10	$\frac{9}{10}$
4	50	$\frac{1}{10}$	5	5	$\frac{4}{5}$
5	2	1	2	2	$\frac{1}{2}$
3,5	60	$\frac{1}{3}$	30	20	$\frac{19}{30}$

$R_1$						
	Relation	n	S	С	Т	rank
R	2	20	$\frac{1}{5}$	4	4	$\frac{3}{4}$
K <sub>3,5</sub>	3	30	$\frac{1}{15}$	10	10	$\frac{9}{10}$
	4	50	$\frac{1}{10}$	5	5	$\frac{4}{5}$
$R_2$	5	2	1	2	2	$\frac{1}{2}$
	3,5	60	$\frac{1}{15}$	30	20	$\frac{19}{30}$
$R_4$						

Subtree  $R_1$ : merging

Denormalizing  $R_1$  $R_3$  $R_5$  $R_2$  $R_4$ 

Relation	n	S	С	Т	rank
2	20	$\frac{1}{5}$	4	4	$\frac{3}{4}$
3	30	$\frac{1}{15}$	10	10	$\frac{9}{10}$
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#### IKKBZ - another example



- ► |*R*<sub>1</sub>| = 30
- ► |*R*<sub>2</sub>| = 100
- ► |*R*<sub>3</sub>| = 30
- ►  $|R_4| = 20$
- ►  $|R_5| = 10$
- ►  $|R_6| = 20$
- ►  $|R_7| = 70$
- ►  $|R_8| = 100$
- $|R_9| = 100$



• 
$$r(R_6) = \frac{9}{10} = 0.9$$

• 
$$r(R_7) = \frac{4}{5} = 0.8$$

• 
$$r(R_8) = \frac{19}{20} = 0.95$$

• 
$$r(R_9) = \frac{3}{4} = 0.75$$

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•  $C(R_{8,9}) = 100$ 

▶ 
$$T(R_{8,9}) = 80$$

► 
$$r(R_{8,9}) = \frac{79}{100} = 0.79$$

• 
$$C(R_{6,7}) = 60$$

• 
$$T(R_{6,7}) = 50$$

• 
$$r(R_{6,7}) = \frac{49}{60} \approx 0.816$$



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- ▶  $n_{5,8,9} = 800$
- $C_{5,8,9} = \frac{1515}{2}$

• 
$$T_{5,8,9} = 600$$

▶  $r(R_{5,8,9}) = \frac{1198}{1515} \approx 0.79$ 

▶ 
$$r(R_{6,7}) \approx 0.816$$



- ▶  $r(R_2) = \frac{9}{10}$
- ▶  $r(R_3) = 0.8$

$$\blacktriangleright r(R_4) = 0$$

▶  $r(R_{5,8,9}) = \frac{1198}{1515} \approx 0.79$ 

▶ 
$$r(R_{6,7}) \approx 0.816$$

#### $R_1 - R_3 - R_4 - R_{5,8,9} - R_{6,7} - R_2$

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#### $R_1 \longrightarrow R_3 \longrightarrow R_4 \longrightarrow R_5 \longrightarrow R_8 \longrightarrow R_9 \longrightarrow R_6 \longrightarrow R_7 \longrightarrow R_2$

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### **IKKBZ**-based heuristics

What if Q has cycles?

 Observation 1: the answer of the query, corresponding to any subgraph of the query graph, is a superset of the answer to the original query

Observation 2: a very selective join is more likely to be influential in choosing the order than a non-selective join

#### **IKKBZ**-based heuristics

What if Q has cycles?

- Observation 1: the answer of the query, corresponding to any subgraph of the query graph, is a superset of the answer to the original query
- Observation 2: a very selective join is more likely to be influential in choosing the order than a non-selective join

Choose the minimum spanning tree (minimize the product of the edge weights), compute the total order, compute the original query.

## Homework: Task 1 (10 points)

Selectivity estimation continues...

- Our estimations (prev. homework) are far from perfect
- Construct specific examples (database schema, concrete instances of relations and selections/joins), where our estimations are very "bad"
- "Bad" means that for some queries (give examples of SQL queries) the logical plan will be suboptimal (w.r.t C<sub>out</sub>), if we use these estimations
- In other words, bad estimations mislead the optimizer and it outputs a clearly suboptimal plan

Two examples (one for selections, one for joins)

## Homework: Task 2 (5 points)

 Give an example query instance where the optimal join tree (using C<sub>out</sub>) is bushy and includes a cross product.

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Note: the query graph should be connected!

## Homework: Task 3 (15 points)

- Using the program from the first exercise as a basis, implement a program that
  - parses SQL queries
  - translates them into tinydb execution plans
  - and executes the query.
- Note: a canonical translation of the joins is fine, but push all predicates of the form attr = const down to the base relations

# Info

- Slides and exercises: http://db.in.tum.de/teaching/ws1617/queryopt/
- Send any questions, comments, solutions to exercises etc. to radke@in.tum.de

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Exercises due: 9 AM, November 21