# Query Optimization 

 Exercise Session 3Bernhard Radke

November 21

## Homework: Task 1

```
select *
    from lineitem l, orders o, customers c
    where l.l_orderkey=o.o_orderkey
    and o.o_custkey=c.c_custkey
    and c.c_name='Customer#000014993'.
```


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The selectivity of $\sigma_{R 1 . x=c}$ is...

- if $x$ is the key:


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The selectivity of $\sigma_{c 1<R 1 . x<c 2}$ is $\frac{c 2-c 1}{\max -\min }$

## Homework: Task 3

- $|R|=1,000$ pages, $|S|=100,000$ pages
- 1 page - 50 tuples, 1 block - 100 pages
- avg. access $=10 \mathrm{~ms}$, transfer speed $=10,000$ pages $/ \mathrm{sec}$
- Time for blocked nested loops join $=$ ?


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- Time for blocked nested loops join $=$ ?
- choose left argument: $R$ vs. $S, \frac{1,000}{100}$ vs. $\frac{100,000}{100} \Rightarrow R$


## Homework: Task 3

- Time to read one block:

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- Repeat it for every block in $R$ :

$$
T_{B N L J}=\frac{\text { \#pages in } \mathrm{R}}{\text { block size }}(10 s) \approx 100 s
$$

## Greedy operator ordering

- take the query graph
- find relations $R_{1}, R_{2}$ such that $\left|R_{1} \bowtie R_{2}\right|$ is minimal and merge them into one node
- repeat until the query graph has more than one node

Generates bushy trees!

## Example



## Example - step 1

## Example - after step 1



## Example - step 2



## Example- after step 2



## Example - step 3



## Example - after step 3



## Example - step 4



## Example - after step 4



## Example - step 5



## Example - after step 5

$\left(R_{1} \bowtie R_{2}\right) \bowtie\left(R_{3} \bowtie R_{4}\right)(1200)$
0.2268
$\left(R_{7} \bowtie R_{8}\right) \bowtie\left(\left(R_{5} \bowtie R_{6}\right) \bowtie R_{9}\right)(1080)$

## Example - result



## IKKBZ (informally)

Query graph $Q$ is acyclic. Pick a root node, turn it into a tree. Run the following procedure for every root node, select the cheapest plan

Input: rooted tree $Q$

1. if the tree is a single chain, stop
2. find the subtree (rooted at $r$ ) all of whose children are chains
3. normalize, if $c_{1} \rightarrow c_{2}$, but $\operatorname{rank}\left(c_{1}\right)>\operatorname{rank}\left(c_{2}\right)$ in the subtree rooted at $r$
4. merge chains in the subtree rooted at $r$, rank is ascending
5. repeat 1

## IKKBZ (informally)

For every relation $R_{i}$ we keep

- cardinality $n_{i}$
- selectivity $s_{i}$ — the selectivity of the incoming edge from the parent of $R_{i}$
- cost $C\left(R_{i}\right)=n_{i} s_{i}$ (or 0 , if $R_{i}$ is the root)
- rank $r_{i}=\frac{n_{i} s_{i}-1}{n_{i} s_{i}}$

Moreover,

- $C\left(S_{1} S_{2}\right)=C\left(S_{1}\right)+T\left(S_{1}\right) C\left(S_{2}\right)$
- $T(S)=\prod_{R_{i} \in S}\left(s_{i} n_{i}\right)$
- rank of a sequence $r(S)=\frac{T(S)-1}{C(S)}$


## Understanding IKKBZ

- what is the rank?
- when is $\left(R_{1} \bowtie R_{2}\right) \bowtie R_{3}$ cheaper than $\left(R_{1} \bowtie R_{3}\right) \bowtie R_{2}$ ?


## Understanding IKKBZ

- what is the rank?
- when is $\left(R_{1} \bowtie R_{2}\right) \bowtie R_{3}$ cheaper than $\left(R_{1} \bowtie R_{3}\right) \bowtie R_{2}$ ?
- if $r\left(R_{2}\right)<r\left(R_{3}\right)$ !


## IKKBZ - example



| Relation | n | s | C | T | rank |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 2 | 20 | $\frac{1}{5}$ | 4 | 4 | $\frac{3}{4}$ |
| 3 | 30 | $\frac{1}{3}$ | 10 | 10 | $\frac{9}{10}$ |
| 4 | 50 | $\frac{1}{10}$ | 5 | 5 | $\frac{4}{5}$ |
| 5 | 2 | 1 | 2 | 2 | $\frac{1}{2}$ |

## IKKBZ - example

Subtree $R_{3}$ : merging,
$\operatorname{rank}\left(R_{5}\right)<\operatorname{rank}\left(R_{4}\right)$


| Relation | n | s | C | T | rank |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 2 | 20 | $\frac{1}{5}$ | 4 | 4 | $\frac{3}{4}$ |
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## IKKBZ - example

Subtree $R_{1}$ : $\operatorname{rank}\left(R_{3}\right)>\operatorname{rank}\left(R_{5}\right)$, normalizing


| Relation | n | s | C | T | rank |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 20 | $\frac{1}{5}$ | 4 | 4 | $\frac{3}{4}$ |
| 3 | 30 | $\frac{1}{3}$ | 10 | 10 | $\frac{9}{10}$ |
| 4 | 50 | $\frac{1}{10}$ | 5 | 5 | $\frac{4}{5}$ |
| 5 | 2 | 1 | 2 | 2 | $\frac{1}{2}$ |
| 3,5 | 60 | $\frac{1}{3}$ | 30 | 20 | $\frac{19}{30}$ |

## IKKBZ - example

Subtree $R_{1}$ : merging


| Relation | n | s | C | T | rank |
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| 2 | 20 | $\frac{1}{5}$ | 4 | 4 | $\frac{3}{4}$ |
| 3 | 30 | $\frac{1}{15}$ | 10 | 10 | $\frac{9}{10}$ |
| 4 | 50 | $\frac{1}{10}$ | 5 | 5 | $\frac{4}{5}$ |
| 5 | 2 | 1 | 2 | 2 | $\frac{1}{2}$ |
| 3,5 | 60 | $\frac{1}{15}$ | 30 | 20 | $\frac{19}{30}$ |

## IKKBZ - example



## IKKBZ - another example

$$
\begin{aligned}
-\left|R_{1}\right| & =30 \\
-\left|R_{2}\right| & =100 \\
-\left|R_{3}\right| & =30 \\
-\left|R_{4}\right| & =20 \\
-\left|R_{5}\right| & =10 \\
-\left|R_{6}\right| & =20 \\
-\left|R_{7}\right| & =70 \\
-\left|R_{8}\right| & =100 \\
-\left|R_{9}\right| & =100
\end{aligned}
$$

## IKKBZ



## IKKBZ

- $C\left(R_{8,9}\right)=100$

$R_{8,9}$
- $T\left(R_{8,9}\right)=80$
- $r\left(R_{8,9}\right)=\frac{79}{100}=0.79$
- $C\left(R_{6,7}\right)=60$
- $T\left(R_{6,7}\right)=50$
- $r\left(R_{6,7}\right)=\frac{49}{60} \approx 0.816$


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- $n_{5,8,9}=800$
- $C_{5,8,9}=\frac{1515}{2}$
- $T_{5,8,9}=600$
- $r\left(R_{5,8,9}\right)=\frac{1198}{1515} \approx 0.79$
- $r\left(R_{6,7}\right) \approx 0.816$


## IKKBZ

- $r\left(R_{2}\right)=\frac{9}{10}$
- $r\left(R_{3}\right)=0.8$
- $r\left(R_{4}\right)=0$
- $r\left(R_{5,8,9}\right)=\frac{1198}{1515} \approx 0.79$
- $r\left(R_{6,7}\right) \approx 0.816$

IKKBZ
$R_{1}-R_{3}-R_{4}-R_{5,8,9}-R_{6,7}-R_{2}$

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## IKKBZ-based heuristics

What if $Q$ has cycles?

- Observation 1: the answer of the query, corresponding to any subgraph of the query graph, is a superset of the answer to the original query
- Observation 2: a very selective join is more likely to be influential in choosing the order than a non-selective join


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- Observation 2: a very selective join is more likely to be influential in choosing the order than a non-selective join

Choose the minimum spanning tree (minimize the product of the edge weights), compute the total order, compute the original query.

## Homework: Task 1 (10 points)

Selectivity estimation continues...

- Our estimations (prev. homework) are far from perfect
- Construct specific examples (database schema, concrete instances of relations and selections/joins), where our estimations are very "bad"
- "Bad" - means that for some queries (give examples of SQL queries) the logical plan will be suboptimal (w.r.t $C_{\text {out }}$ ), if we use these estimations
- In other words, bad estimations mislead the optimizer and it outputs a clearly suboptimal plan
- Two examples (one for selections, one for joins)


## Homework: Task 2 (5 points)

- Give an example query instance where the optimal join tree (using $C_{\text {out }}$ ) is bushy and includes a cross product.
- Note: the query graph should be connected!


## Homework: Task 3 (15 points)

- Using the program from the first exercise as a basis, implement a program that
- parses SQL queries
- translates them into tinydb execution plans
- and executes the query.
- Note: a canonical translation of the joins is fine, but push all predicates of the form attr $=$ const down to the base relations


## Info

- Slides and exercises: http://db.in.tum.de/teaching/ws1617/queryopt/
- Send any questions, comments, solutions to exercises etc. to radke@in.tum.de
- Exercises due: 9 AM, November 21

